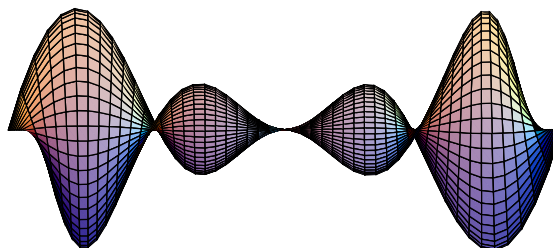


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***Problems in Mathematics  
&  
Experiments with Mathematica***



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[Title page](#)

**Authors**

**Preface**

[How to use the book](#)

[Notations](#)

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**1. [A short introduction to Mathematica](#)**

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**2. Elementary Functions**

2.1 [Sets, numbers, Cartesian systems](#)

2.2 [Basic properties of functions](#)

2.3 [Powers](#)

2.4 [Trigonometric functions](#)

2.5 [Exponential and logarithmic functions](#)

2.6 [Exercises on elementary functions](#)

2.7 [Inverse function](#)

2.8 [Elementary transformations](#)

2.9 [Logarithmic transformations](#)

2.10 [Other transformations](#):  $|f(x)|$ ,  $\frac{1}{f(x)}$ ,  $f\left(\frac{1}{x}\right)$

---

**3. Limit and continuity**

3.1 [Definitions and graphic meaning](#)

3.2 [Basic rules and techniques: polynomials and rational fractions](#)

3.3 [Inequalities, applications of](#)  $\lim_{x \rightarrow 0} \frac{\sin(x)}{x} = 1$

3.4 [Simple and compound growths. The limit](#)  $\lim_{x \rightarrow 0} \left(1 + \frac{1}{x}\right)^x = e$

3.5 [Comparison of growths](#)

---

## 4. The derivative and its applications

4.1 [Definition, geometrical meaning, tangent line](#)

4.2 [Differentiation rules](#)

4.3 [Linear approximation](#)

4.4 [Approximation of zeros](#)

4.5 [L'Hospital rule to find limit of fractions](#)

4.6 [Extremal values, monotony, concavity and investigation of functions](#)

4.7 [Taylor polynomials, Taylor series](#)

---

## 5. Indefinite integral

5.1 [Definition, geometrical meaning, properties](#)

5.2 [Integration techniques](#)

5.3 [Find a particular antiderivative](#)

---

## 6. Definite integral

6.1 [Definition, geometrical meaning, properties](#)

6.2 [Formal integration: Newton-Leibniz formula](#)

6.3 [Numerical integration: Integral approximation formulas](#)

6.4 [Applications](#)

---

## 7. 1D Ordinary differential equations

7.1 [Definitions, properties, vectorfield, equilibria](#)

7.2 [Mathematica tools to solve a differential equation](#)

7.3 [Linear equations](#)

7.4 [The equation  \$x' = k\(A-x\)\(B-x\)\$](#)

---

## 8. Vector-valued functions, parametric curves and surfaces

8.1 Drawing, properties

8.2 Applications

---

## 9. Functions of several variables

9.1 [Basic properties: definition, domain, graph, contours](#)

9.2 [Partial derivatives](#)

9.3 [Finding a local extremum](#)

9.4 [Curve-fitting by the least square, linear regression](#)

---

## 10. Appendix: Labs

### 10.1 [The volume of cylindrical bodies](#)

### 10.2 [Experiments with 1D ODE-s](#)

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