

Practice, confidence intervals

1. Confidence interval for the population mean (μ), if population standard deviation (σ) is known.

1.1. The mean height of first year pharmaceutical students is 175 cm with SD= 10. Let's suppose the height follow normal distribution with these parameters.

- What percentage of the height is above 175 cm.....
- What percentage of the height is below 175 cm? $P(\text{height} < 175) = \dots\dots\dots$
- What percentage of the height are between 155 and 195?
- What percentage of the height is below 155 cm?

1.2. Calculate the mean and standard error of mean of a sample of 36 cases derived from this population
Mean..... S.E.....

1.3 The mean of another random sample with 36 number of cases is 172 and SD=10. Calculate the 95% confidence interval.....

What is the meaning of the 95% CI?

Compare the population mean (175) with the 95% CI calculated. It is included in the 95% CI?.....

2. Confidence interval for the population mean (μ), if population standard deviation (σ) is unknown.

2.1. (Example from Altman). In a trial we actually observed a mean serum albumin of 34.46 g/l with a standard error of 1.273 g/l from a sample of 21 patients with primary biliary cirrhosis. Find the 95% confidence interval.

$\alpha =$

N=

Mean=

SE=

Degrees of freedom=

$t_{\alpha} =$

Mean - t_{α} SE=

Mean + t_{α} SE=

Confidence interval:

Meaning:

$P(\dots\dots\dots < \text{true population mean} < \dots\dots\dots) = 0.95$

We can be 95% confident from this study that the true mean serum albumin among all such patients lies somewhere in the range 31.8 to 37.1 g/l, with 34.46 as our best estimate. This interpretation depends on the assumption that the sample of 21 patients is representative of all patients with the disease.

2.2. Find the 99% confidence interval

$\alpha =$

N=

Mean=

SE=

Degrees of freedom=

$t_{\alpha} =$

Mean - t_{α} SE=

Mean + t_{α} SE=

Confidence interval:

Meaning:

$P(\dots\dots\dots < \text{true population mean} < \dots\dots\dots) = 0.99$

2.3. Suppose that the above data were observed from a sample of 216 patients. Find the 95% confidence interval.

$\alpha =$

$N =$

Mean =

SE =

Degrees of freedom =

$t_{\alpha} =$

Mean - t_{α} SE =

Mean + t_{α} SE =

Confidence interval:

Meaning:

$P(\dots < \text{true population mean} < \dots) = 0.95$

2.4. In a study, systolic blood pressure of 10 healthy women was measured. The mean was 119, the standard error 0.664. Calculate the 95% confidence interval for the population mean!

($\alpha = 0.05$, $t_{\text{tabla}} = 2.26$).

2.5. In a study, systolic blood pressure of 10 healthy women was measured. The mean was 119, the standard error 2.1. Calculate the 95% confidence interval for the population mean!

($\alpha = 0.01$, $t_{\text{tabla}} = 2.26$).

Compare the length of this last confidence interval to the earlier one (in Problem 2.4.).

..... Explain

Questions

1. Which is wider, a 95% or a 99% confidence interval?
2. When you construct a 95% confidence interval, what are you 95% confident about?
3. When computing a confidence interval, when do you use t -table and when do you use u ?

Practice with SPSS:

Open the data file of the questionnaire filled out by the students in SPSS! (Data:E/Data/Biostat=kerd??.sav) or QUEST2010.sav.

1. Examine the distribution of "age"!

Find the 95% CI.....

Find the 99% CI.....

With 95% probability, can we state that the mean age in the population of students is 20?.....

Explain.....

With 99% probability, can we state that the mean age in the population of students is 20?.....

Explain.....

2. Examine the distribution of "body height" for boys and girls!

Find the 95% CI for boys girls

Find the 99% CI for boys girls

With 95% probability, can we state that the mean body height in the population of girls is 160 cm?

Explain.....

With 95% probability, can we state that the mean body height in the population of boys is 160 cm?

Explain.....

With 99% probability, can we state that the mean body height in the population of girls is 160 cm?

Explain.....

With 99% probability, can we state that the mean body height in the population of boys is 160 cm?

Explain.....